

## REVIEW AND SYNTHESIS

# Modelling dendritic ecological networks in space: an integrated network perspective

Erin E. Peterson,<sup>1\*</sup> Jay M. Ver Hoef,<sup>2</sup> Dan J. Isaak,<sup>3</sup> Jeffrey A. Falke,<sup>4</sup> Marie-Josée Fortin,<sup>5</sup> Chris E. Jordan,<sup>6</sup> Kristina McNyset,<sup>4</sup> Pascal Monestiez,<sup>7</sup> Aaron S. Ruesch,<sup>8,9</sup> Aritra Sengupta,<sup>10</sup> Nicholas Som,<sup>11,12</sup> E. Ashley Steel,<sup>13</sup> David M. Theobald,<sup>14</sup> Christian E. Torgersen<sup>15</sup> and Seth J. Wenger<sup>16</sup>

### Abstract

Dendritic ecological networks (DENs) are a unique form of ecological networks that exhibit a dendritic network topology (e.g. stream and cave networks or plant architecture). DENs have a dual spatial representation; as points within the network and as points in geographical space. Consequently, some analytical methods used to quantify relationships in other types of ecological networks, or in 2-D space, may be inadequate for studying the influence of structure and connectivity on ecological processes within DENs. We propose a conceptual taxonomy of network analysis methods that account for DEN characteristics to varying degrees and provide a synthesis of the different approaches within the context of stream ecology. Within this context, we summarise the key innovations of a new family of spatial statistical models that describe spatial relationships in DENs. Finally, we discuss how different network analyses may be combined to address more complex and novel research questions. While our main focus is streams, the taxonomy of network analyses is also relevant anywhere spatial patterns in both network and 2-D space can be used to explore the influence of multi-scale processes on biota and their habitat (e.g. plant morphology and pest infestation, or preferential migration along stream or road corridors).

### Keywords

Connectivity, dendritic ecological network, directionality, network analysis, scales, spatial statistics, stream network, taxonomy of network analyses.

*Ecology Letters* (2013) 16: 707–719

## INTRODUCTION

The use of network frameworks and analyses to gain a better understanding of ecological structure and function has dramatically increased in recent years (Proulx *et al.* 2005; Dale & Fortin 2010). Network models, such as graph-theoretic-based approaches (Urban *et al.* 2009), are simplifications of reality used to conceptualise and describe relationships, either qualitatively or quantitatively, between a set of components interacting as an ecological system. Such topological structures have been used implicitly and explicitly in metapopulation (Hanski 1998), metacommunity (Cadotte 2006), and metaecosystem models (Massol *et al.* 2011). The appeal of a network-based approach across a suite of ecological and evolutionary systems stems from the explicit emphasis on the functional relationships (e.g. edges, links) between the entities of interest (e.g. nodes,

points, patches). Hence, the same network framework can be used to investigate the effects of various processes, such as gene flow (Fortuna *et al.* 2009), predator–prey relationships (Bascompte *et al.* 2005) or energy fluxes (Proulx *et al.* 2005), between nodes (e.g. individuals, populations, communities). These network models are commonly applied to ecological phenomenon represented non-spatially, such as multitrophic interactions at a single location or area (e.g. Bascompte *et al.* 2005). In other cases, physical space is treated as a network (Gilarranz & Bascompte 2012), with nodes representing spatially explicit habitat patches, and edges denoting processes such as the rate of dispersal between habitat patches (Muneepeerakul *et al.* 2008) or a georeferenced dispersal pathway (Fall *et al.* 2007).

Dendritic ecological networks (DENs; Grant *et al.* 2007) are used to describe spatial relationships in ecosystems that naturally exhibit a physical dendritic network topology (e.g. stream and cave

<sup>1</sup>CSIRO Division of Mathematics, Informatics and Statistics, Dutton Park, QLD, Australia

<sup>2</sup>NOAA National Marine Mammal Laboratory, Seattle, WA, USA

<sup>3</sup>USDA Forest Service, Rocky Mountain Research Station, Boise, ID, USA

<sup>4</sup>Department of Fisheries and Wildlife, Oregon State University, Corvallis, OR, USA

<sup>5</sup>Department of Ecology & Evolutionary Biology, University of Toronto, Toronto, ON, Canada

<sup>6</sup>NOAA/NMFS/NWFSC Conservation Biology Division, Seattle, WA, USA

<sup>7</sup>Inra, Unité Biostatistique et Processus Spatiaux, Avignon, France

<sup>8</sup>School of Environmental and Forest Sciences, University of Washington, Seattle, WA, USA

<sup>9</sup>Present address: Wisconsin Department of Natural Resources, Madison, WI, USA

<sup>10</sup>Department of Statistics, The Ohio State University, Columbus, OH, USA

<sup>11</sup>Department of Forest Ecosystems and Society, Oregon State University, Corvallis, OR, USA

<sup>12</sup>Present address: U.S. Fish and Wildlife Service, Arcata, CA, USA

<sup>13</sup>USDA Forest Service, Pacific Northwest Research Station, Seattle, WA, USA

<sup>14</sup>Department of Fish, Wildlife & Conservation Biology, Colorado State University, Fort Collins, CO, USA

<sup>15</sup>U.S. Geological Survey, Forest and Rangeland Ecosystem Science Center, Cascadia Field Station, School of Environmental and Forest Sciences, University of Washington, Seattle, WA, USA

<sup>16</sup>Trout Unlimited, Boise, ID, USA

\*Correspondence: E-mail: Erin.Peterson@csiro.au

networks or plant architecture). A number of characteristics differentiate DENs from other types of ecological networks (Grant *et al.* 2007). First, movement of organisms, material or energy is primarily restricted to the physical network, which forms ecological corridors (Rodríguez-Iturbe *et al.* 2009). However, the permeability of these ecological corridors varies depending on the organism or process of interest. For example, troglobites may never move outside of a cave network (Barr & Holsinger 1985), while semi-aquatic organisms living in, or nearby streams may also move across the terrestrial landscape (Carranza *et al.* 2012). Second, DENs have fewer redundant pathways compared to other non-spatial or spatially structured ecological networks; though braiding may occur in some stream or cave networks. Third, directionality may also be important in some DENs, such as cave and stream networks, where flowing water strongly influences physicochemical and biological processes. Fourth, biological and physicochemical processes are not restricted to nodes, with relationships between nodes represented as edges; instead, processes occur *on* the network in DENs. For example, the availability and spatial arrangement of in-stream habitat may influence the potential distribution of a fish species, while the branching structure of the network affects in-stream dispersal to those habitats and resulting species interactions (e.g. competition and predation; Angermeier *et al.* 2002). Given the unique characteristics of DENs and the spatial complexity of processes on the physical network, many analytical methods used to quantify relationships in other types of ecological networks, or in 2-D space, are unsuitable for studying the influence of structure and connectivity on physicochemical and biological processes in these systems (Grant *et al.* 2007).

A variety of methods can be used to analyse DEN data, but they are scattered across the literature, ranging from graph-theoretic approaches (Dale & Fortin 2010), semivariogram analyses (Ganio *et al.* 2005), to metapopulation modelling (Fagan 2002). Thus, many researchers may be unfamiliar with these methods, as well as, the software needed to implement them. Instead, parametric statistical methods are commonly used to analyse DEN data, which either ignore spatial relationships altogether, or assume that proximity and connectivity are adequately described using Euclidean distance (e.g. ignore network topology). When these methods are used the implicit assumption is that topological relationships within the network are unimportant. Thus, there is a mismatch between conventional analytical approaches and the evolving ecological conceptualisation of DENs. This disparity limits our understanding of how DENs function, weakens our ability to make accurate and unbiased predictions of DEN attributes, and ultimately reduces the effectiveness of management actions in these unique ecosystems.

Our aim is to present a conceptual taxonomy of existing network analyses, which allows us to describe the characteristics of, and draw distinctions between, approaches used to describe network structure and connectivity within DENs. Within this context, we describe in more detail a new class of spatial statistical models for DENs that addresses a significant gap in previous approaches, with potential extensions to these methods. Finally, we discuss ways to combine different network analyses so that more complex and novel research questions may be explored. We mainly focus on freshwater stream networks because they are a common form of DEN (Box 1) and play a significant role in structuring spatio-temporal patterns and processes in both aquatic and terrestrial systems (Paola *et al.* 2006). In addition, human water security and threats to aquatic biodiversity are a major global concern (Vörösmarty *et al.*

### Box 1 Stream ecosystems as dendritic ecological networks

Most studies in lotic freshwater ecology (i.e. flowing, freshwater streams) have been undertaken at two disparate scales (Angermeier *et al.* 2002; Fausch *et al.* 2002): local studies of abundance or biotic interactions at discrete locations ( $\leq 200$  m), and macro-scale studies ( $> 100$  km), which often use coarse, catchment or stream network averages to provide inference about species distributions, evolutionary process, and more recently, climate change impacts (e.g. Sanderson *et al.* 2009). However, key biological and physical processes, such as metapopulation dynamics and disturbance regimes, are thought to operate at intermediate scales (Schlosser & Angermeier 1995; Ward 1998; Fausch *et al.* 2002; Benda *et al.* 2004), where detailed information is often lacking (Falke & Fausch 2010). This is also the scale at which conservation agencies and managers typically perceive the landscape and interact to prioritise conservation actions (Fausch *et al.* 2002). As a result, a spatially continuous view of streams and rivers over intermediate scales (1–100 km; Fausch *et al.* 2002) within the dendritic ecological network (DEN; Grant *et al.* 2007) is needed to better understand key physicochemical and biological processes (Schlosser & Angermeier 1995; Fisher 1997; Ward 1998; Fausch *et al.* 2002; Power & Dietrich 2002; Wiens 2002; Benda *et al.* 2004; Fisher *et al.* 2004). The terminology used to express these ideas is usually different than the terminology used in graph or metapopulation theory, but the goals are similar; to learn about ecosystem processes by investigating relationships among a set of components, or locations, rather than treating discrete locations independently (Proulx *et al.* 2005). Therefore, we refer to this intermediate scale as the ‘network scale’ or ‘network perspective’.

Fundamentally important characteristics of streams, such as their dendritic network structure, connectivity, stream-flow direction and spatio-temporal variability of in-stream habitat and flow, are particularly influential at the network scale. For example, the catchment (land area that a stream network drains) provides nutrient inputs to streams (i.e. lateral connectivity), where in-stream processes alter the form and concentration of those nutrients, which are then transported downstream (i.e. longitudinal connectivity; Finlay *et al.* 2011). In turn, mobile organisms such as fishes and amphibians respond to the spatio-temporal arrangement of conditions within or along the network (Fausch *et al.* 2002), which forms semi-restrictive corridors for the transport of water, materials and organisms (Grant *et al.* 2007). Barriers such as dams and water diversions may also cause longitudinal fragmentation in the network (Ward 1998), making it challenging for relatively mobile organisms to complete life histories across stream networks (Schlosser & Angermeier 1995). In addition, food-web structure and trophic dynamics may vary depending on network structure, position within the catchment and lateral connectivity (e.g. predation by terrestrial organisms; Power & Dietrich 2002). Despite the conceptualisation of stream networks as directed and highly connected DENs, there are few studies that have successfully incorporated all of these fundamentally important stream characteristics into network-scale analyses.

2010). Nevertheless, the concepts are also applicable to other DENs, and in some cases, other spatially structured ecological networks.

## CONCEPTS

### A coordinate system for DENs

A key concept, when modelling DEN data, is that observations have a dual spatial representation; as points within the network (topology) and as points in 2-D space (geography). Figure 1 illustrates this concept using a minimum planar graph (Fall *et al.* 2007), but topology and geography could be represented in other ways. At a minimum, the network perspective requires a dual coordinate system (Fig. 1a), with the DEN represented as a network (Fig. 1b), embedded within the 2-D geographical environment (Fig. 1c). Although it may be simpler to explore network organisation in spatial ecosystems without explicitly representing geography, critical information about ecosystem function may be lost when models fit to DEN data do not adequately account for the dual coordinate system. This concept will be further explored in subsequent sections, but it is worth noting that the need for a dual spatial representation is not a new idea; a measurement always has 2-D coordinates because it is physically collected in geographical space. A variety of conceptual (Schlosser & Angermeier 1995; Fausch *et al.* 2002; Benda *et al.* 2004), metapopulation (Fisher 1997; Hanski 1998; Fagan 2002; Fisher *et al.* 2004; Munepeeraikul *et al.* 2008) and graph-theoretic-based models (Urban & Keitt 2001; Urban *et al.* 2009; Dale & Fortin 2010; Gilarranz & Bascompte 2012; Jabot & Bascompte 2012) have been used to account for the dual coordinate system. However, it is worth re-emphasising this concept because ecological data continue to be modelled solely within network space, in 2-D space, or independent of space altogether.

The dual spatial representation makes modelling DEN data more complex than data represented solely in 2-D or network space. For example, 2-D space simply forms the coordinate system for obtaining samples, which is consistent across study areas (i.e. the same coordinate system). In contrast, the branching structure and connectivity represented by network space is likely to differ and, as a subspace of 2-D, has interesting properties in its own right. When network properties are inadequately described, the analysis and

results may be confounded. For example, data located in the same network space, but resulting from different processes are likely to produce different results (Peterson *et al.* 2006); yet data collected from different networks, but resulting from the same process may also provide different results (Fagan 2002). It is this complex interplay between 2-D and network space, as well as the need to separate and understand their influence on ecological processes that makes a taxonomy of network analyses necessary.

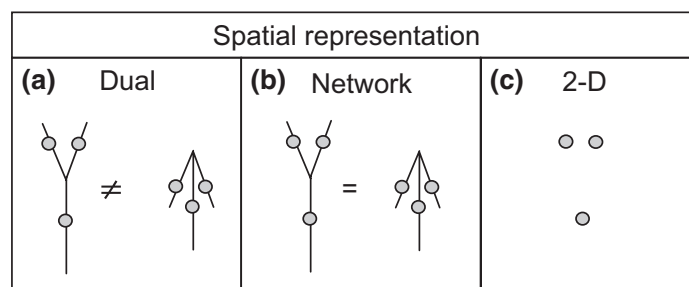
### A taxonomy of network analyses

A wide range of data types has been used to describe the physical structure of DENs, as well as the structure and function of ecological processes. These data types fall into three general categories: (1) physical network structure, (2) physicochemical and biological processes and (3) an aggregation of structure or process (Table 1). Metrics describing structure can be further sub-divided into those describing the network as-a-whole (e.g. drainage density: the total length of the network divided by catchment area) or the sub-network (e.g. stream order: a measure of upstream branching complexity). Various methods have been used to analyse these data types, which we classify as **non-**, **about-**, **on-**, **over-** and **across-**network analysis methods (Table 1, Fig. 2). This taxonomy of network-analysis methods is not meant to drive or be organised by ecological or biological question. Instead, it acts as a pragmatic framework to help ecologists understand the similarities and differences between analytical methods commonly used to analyse ecological processes in stream networks and other DENs.

#### NON-network analysis

A **non-**network analysis ignores the structure, connectivity and directionality of the network (Fig. 2b). Although not technically a network analysis, **non-**network warrants mention because many studies conducted at landscape to regional scales ignore spatial relationships between locations altogether (e.g. regression; Pandey *et al.* 2012). In fewer cases, spatial statistical models based on a 2-D coordinate system (Fig. 1c; Box 2) are used to account for spatial dependence between observations (Yuan 2004). Results and conclusions from many of these studies may be adversely affected by ignoring the properties of stream networks, as we demonstrate in the *Spatial Statistical Methods for Network Analysis* section.

Many researchers attempt to overcome the limitations of **non-**network analyses by including covariates that represent sub-network structure (Hitt & Angermeier 2008), direction and connectivity (Dunham & Rieman 1999; Isaak *et al.* 2007; Flitcroft *et al.* 2012; Table 1). For example, Hitt & Angermeier (2008) quantified the structural position of each survey site relative to the main stem based on stream network topology and then used Mann–Whitney *U*-tests to determine whether fish metrics in headwater tributaries (small segment at the periphery of the network) differed from main tributaries (larger segment draining to the main stem). Other metrics representing habitat quality, proximity, connectivity and arrangement are typically measured using least-cost path analyses and moving-window approaches (Le Pichon *et al.* 2006), or patch size, composition and distance measures (Dunham & Rieman 1999; Isaak *et al.* 2007). Incorporating measures of sub-network structure as covariates in **non-**network analyses allows researchers to explore specific questions relating to the influence of physical network structure and in-stream habitat on physicochemical and biological stream pro-



**Figure 1** Locations within a stream network can be characterised using a (a) dual, (b) network or (c) 2-D spatial representation. A 2-D coordinate system lacks information about network connectivity. A network coordinate system only uses relative position within the network, not the 2-D coordinates; thus, distances between points within the network are equal in (b) and in that sense they are equivalent network structures. A dual representation combines the 2-D coordinate system with the network coordinate system. Various statistical models use none, one or both coordinate systems.

## Box 2 Review of spatial statistics and the spatial linear-mixed model

Spatial autocorrelation, or autocovariance, is the degree to which measurements are similar as a function of the distance separating them (i.e. separation distance). It is inherent in geographical and environmental data sets and occurs in both aquatic and terrestrial systems at multiple scales (Peterson *et al.* 2006; Peterson & Ver Hoef 2010). Spatial statistical modelling is a well-established branch of statistics that provides a convenient way to model these spatial dependencies (Cressie 1993; Diggle *et al.* 1998). As an example, we present a spatial linear-mixed model in the usual vector/matrix form,

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{z} + \boldsymbol{\varepsilon} \quad (1)$$

where  $\mathbf{y}$  is a vector of random variables (i.e. the response variable) measured at multiple locations on the stream network(s),  $\mathbf{X}$  is a design matrix for fixed effects, which contains the covariates (i.e. explanatory variables),  $\boldsymbol{\beta}$  is a vector of parameters for the fixed effects (i.e. regression coefficients),  $\mathbf{z}$  is a vector of random variables that are spatially correlated and  $\boldsymbol{\varepsilon}$  is a vector of independent random errors. The linear model is convenient because it decomposes data into three components: (1) covariates that are measured in the field or remotely, which may be spatially patterned themselves in  $\mathbf{X}\boldsymbol{\beta}$  (e.g. percent shade at a location, land use or climate); (2) unmeasured spatially patterned covariates as random variation in  $\mathbf{z}$ ; these include factors that are known to be influential, but were not measured (e.g. land use or biotic interactions), as well as unknown factors resulting from a lack of understanding about the process; and (3) independent errors, including measurement errors (e.g. calibration error), in  $\boldsymbol{\varepsilon}$ .

An autocovariance function is simply the covariance between any two values from  $\mathbf{z}$  as a function of separation distance, controlled by the covariance parameters. Three parameters are commonly used to describe the variance structure of the spatial linear model (1): the nugget effect, the partial sill and the range. The nugget effect is the variance of  $\boldsymbol{\varepsilon}$  and describes the variation between sites as the separation distance approaches zero. This may be due to variation at a scale finer than the shortest separation distance or measurement error. The variance of  $\mathbf{z}$  is called the partial sill and it is the spatially structured component of the random variation that is modelled. Note that, together the partial sill and nugget make up the sill, which represents the overall variance. Finally, the range parameter describes how fast autocorrelation decays to zero between any two values from  $\mathbf{z}$  (e.g. the distance within which spatial autocorrelation is expected to occur).

When ecological processes are autocorrelated, a spatial statistical approach provides parameter estimates with the proper amount of uncertainty, whereas wrongly assuming independence often means that significant relationships may be identified that do not exist (Cressie 1993). In addition, spatial statistical models use autocorrelation to make better local predictions, with estimates of uncertainty at unobserved locations. An in-depth discussion of spatial statistical models can be found in Cressie (1993).

cesses. The assumption is that the structure of the network either affects the process directly (e.g. upstream dispersal in a branching network) or acts as a surrogate for a process (e.g. magnitude of changes to flow downstream after a localised rain event) (Fisher *et al.* 2004). However, it is unlikely that the complexity of multi-scale spatial processes and interactions within the dual coordinate system (Wiens 2002) can be adequately represented through spatially explicit covariates alone. Instead, observed patterns result from the *combined* effects of in-stream flow and habitat, connectivity and trophic interactions, as well as, the physical structure of the network.

### *ABOUT-network analysis*

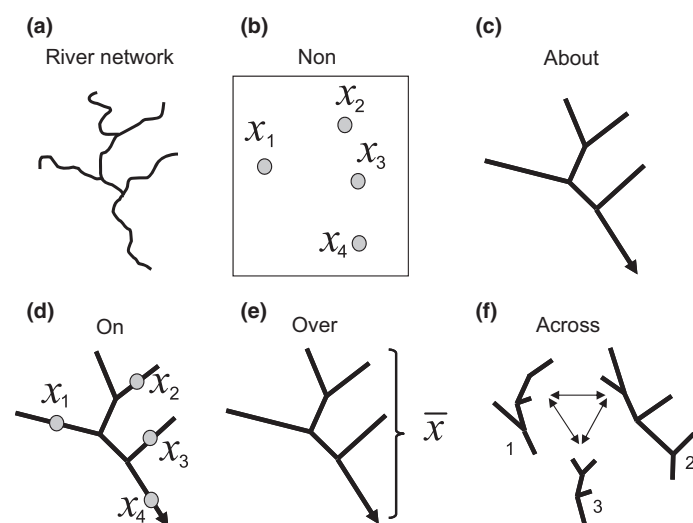
Many statistical methods have been developed for **about**-network analyses (Kolaczyk 2009), where the primary focus is the physical structure and/or connectivity of the network itself (Table 1; Fig. 2c). Most methods were designed to model networks that do not exist in 2-D space, such as social or internet networks, and simply account for network space; though, these non-spatial networks are often  $N$ -dimensional graphs, which are affected by spatial scale. Graph-theoretic methods represent a classic **about**-network approach (Rayfield *et al.* 2011), which can be modified to account for a dual coordinate system (Dale & Fortin 2010). Graph-based approaches are uncommon in stream ecology, but may provide a better understanding about species movement and persistence, as well as informing spatially targeted restoration activities (Erös *et al.* 2011; Fullerton *et al.* 2011; Carranza *et al.* 2012). For example, Schick & Lindley (2007) used graph-theoretic metrics, including degree, edge weight and node strength, to test how directional connectivity influences the structure of fish populations. **About**-network analyses for a dual coordinate system (Fig. 1a) also have a long history in fluvial geomorphology (Horton 1945), where descriptors of network structure were derived to describe landscape evolution and understand scaling properties (e.g. stream order). Many of these descriptors have been used to understand the influence of structure on physicochemical or biological patterns in streams (Fagan 2002; Fisher *et al.* 2004). For example, the *Network Dynamics Hypothesis* (Benda *et al.* 2004) describes how multi-scale about-network characteristics may interact with stochastic disturbances to structure habitat, biological diversity and productivity. In addition, well-known **about**-network measures, such as the fractal dimension and drainage density, may be used to quantitatively describe the structural characteristics of the entire network, while newer measures, such as the dendritic connectivity index, may be used to assess **about**-network connectivity (Cote *et al.* 2009).

### *ON-network analysis*

**On**-network analyses (Fig. 2d) are based on point data, which describe physical sub-network structure, as well as physicochemical and/or biological processes or attributes (Table 1). The majority of **on**-network analyses have been used to investigate the influence of network structure on fragmentation, the movement behaviour of organisms, population distribution and metapopulation persistence (Fagan 2002; Grant *et al.* 2007; Carrara *et al.* 2012), as well as, the combined effects of structure and temporal variation in mortality on competitive metacommunity dynamics (Auerbach & Poff 2011).

**Table 1** A description of network data types and the potential network analysis methods that can be used to analyse them

Data type	Examples	Analysis method				
		NON	ABOUT	ON	OVER	ACROSS
Physical network structure (whole network)	Drainage density, fractal dimension or metric of network connectivity		✓			✓
Physical network structure (sub-network)	Confluence angle, stream order, node degree, edge weight, patch connectivity or composition	✓	✓	✓	✓	
Physicochemical and biological processes or attributes	Pool depth, pH or fish counts	✓		✓	✓	
Structure and processes aggregation	A special case where measurements are aggregated over an area (e.g. a hydrologic unit), a network, or multiple networks Mean fish count or confluence angle				✓	✓



**Figure 2** (a) A real stream is represented as a network embedded in 2-D space. (b) **Non**-network analyses use explicitly sampled values in 2-D space, but they make no use of the network structure. (c) Analyses **about** a network look at characteristics of the network structure such as segment lengths, branching and connectivity. (d) Analyses **on** a network use explicitly sampled values at points in network space. (e) Analyses **over** a network average or aggregate the spatially explicit point values, whereas (f) analyses **across** networks compare network values, either about or over the individual networks.

These studies account for the dual spatial representation of streams data and as a result have significantly improved our theoretical understanding of the relationship between network structure, connectivity and function. From a practical standpoint, these findings are now being used to assess management-related questions specifically focused on physical changes to connectivity, such as interbasin transfers (Grant *et al.* 2012). However, to our knowledge they have not been used to address issues such as the influence of land-management practices on in-stream habitat and organismal distributions, in a spatially explicit manner. For example, lateral connectivity with the terrestrial landscape is generally not considered, movement through the network is mainly treated as a function of distance (see Goldberg *et al.* 2010 for an exception), and restrictions to organismal movement due to within-network habitat heterogeneity are not represented (Grant *et al.* 2007).

**On**-network analyses that use measurements of physicochemical and biological processes are less common than those based on descriptive metrics of sub-network structure. Mantel tests (Mantel

1967) and partial Mantel tests (Smouse *et al.* 1986) are **on**-network approaches commonly used to investigate the differences in beta diversity among sites based on various distance measures. However, Legendre & Fortin (2010) showed that alternative methods, such as regression or canonical redundancy analysis, had more statistical power when the goal was to investigate relationships between species similarity/dissimilarity and environmental variables. More recently, a new family of spatial statistical models (i.e. spatial linear regression) has been developed for **on**-network analyses (Ver Hoef *et al.* 2006), which account for the structure, connectivity, direction and dual spatial representation of streams (see Box 2 for an introduction to spatial statistical models). To date, these models have not been used to investigate the influence of network structure on stream processes. Instead, they have been applied to better understand the influence of catchment characteristics on in-stream processes (Gardner & McGlynn 2009; Isaak *et al.* 2010) or to make predictions at unobserved locations, with estimates of uncertainty (Cressie *et al.* 2006; Garreta *et al.* 2010; Isaak *et al.* 2010). The model predictions have also been used for a variety of purposes including the assessment of in-stream thermal suitability (Ruesch *et al.* 2012) and to provide spatially explicit estimates for broad-scale monitoring (Garreta *et al.* 2009; Money *et al.* 2009a,b). These **on**-network methods are similar to traditional linear regression techniques commonly applied to point measurements in stream ecology; except that the assumption of independent errors is replaced with the notion that random errors co-vary in both 2-D and network space. These concepts will be further explored in the *Spatial Statistical Methods for Network Analysis* section.

#### OVER-network analysis

Data describing the physical network structure, physicochemical and biological processes or an aggregation of those characteristics within an area or feature may be summarised **over** a network or multiple networks (Table 1; Fig. 2e). The complexity of the **over**-network analysis depends on data type and spatial representation (Fig. 1). For example, measurements describing physical structure at single time points, such as confluence angles (the angle of two stream segments converging) calculated from a static geographic information system (GIS) data set, do not have a variance; therefore, a simple **over**-network summary (e.g. mean) may be sufficient. However, biological or physicochemical measurements (e.g. stream temperature) are temporally dynamic and each has their own variance, which can be summarised **over** the network(s). For instance, empirical semi-variogram analysis has been used to explore **over**-network spatial

dependency of *Oncorhynchus clarki clarki* (coastal cutthroat trout) counts in western Oregon as a function of hydrologic (i.e. in-stream) distance (Ganio *et al.* 2005). Multiple **over-network** patterns of spatial dependency may also be evaluated separately for network and 2-D space, allowing spatial patterns across the dual coordinate system to be explored simultaneously (Isaak *et al.* 2010). Another example is block kriging, which can be used to scale up an **on-network** model to an **over-network** analysis (Ver Hoef *et al.* 2006).

#### *ACROSS-network analysis*

An **across-network** analysis is used to compare or contrast characteristics between whole networks or sets of networks (Fig. 2f). The analysis generally takes two forms, depending on whether it is based on data describing the whole-of-network structure (a single measurement without a variance estimate) or data that have been aggregated previously using an **over-network** analysis (estimates with a standard error) (Table 1). **Across-network** analyses are relatively simple for whole-of-network structure data measured at a single time point; a *t*-test could be used to compare two types of networks, while an ANOVA may be appropriate when whole networks can be categorised (e.g. catchment size or climatic region), assuming proper transformations. When an **across-network** analysis is based on aggregated measurements of sub-network structure or physicochemical or biological processes, these data will have an associated variance measure. In that case, statistical models that incorporate measurement error (i.e. uncertainty or variance in the data value), such as a Bayesian hierarchical model (Cressie *et al.* 2009), should be employed. For example, the mean heavy metal concentration in networks draining mined and unmined catchments could be obtained by block kriging point samples, after which a hierarchical model that uses the means and variances from the block kriging model could be used in the **across-network** analysis.

### SPATIAL STATISTICAL METHODS FOR NETWORK ANALYSIS

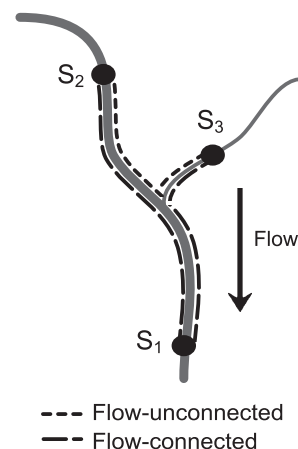
As we examined the literature and developed the taxonomy described above, it was clear that most research that explicitly acknowledges fundamental stream characteristics has been based on **about-** or **on-network** models that use sub-network data structures. Data describing stream-network structure are readily available at broad spatial scales via remote sensing or GIS data sets and may be used with all of the network-analysis methods (Table 1). The primary focus of these studies has been to investigate the influence of physical network structure on biological processes, such as dispersal (Fagan 2002; Schick & Lindley 2007). In contrast, **on-** or **over-network** models fitted to measurements of point data representing physicochemical and/or biological processes are needed to study the effects of stream processes on another physicochemical or biological response; for example, the influence of heterogeneous in-stream water quality on organismal distributions. These studies are less common because near-continuous, network-wide data sets describing in-stream processes are rare (Falke & Fausch 2010). Spatial statistical methods fill a number of needs that are not addressed by other network analysis methods; they can be applied to spatially dependent data and may be used to generate near-continuous, within-network predictions of physicochemical and biological processes (Cressie 1993). This is especially important in DENs, where processes occur *on* the network (Grant *et al.* 2007). Consequently, in this section, we further explore **on-** and

**over-network** analyses using spatial statistical methods, which were briefly described in the *On Network Analysis* and *Over-Network Analysis* sections.

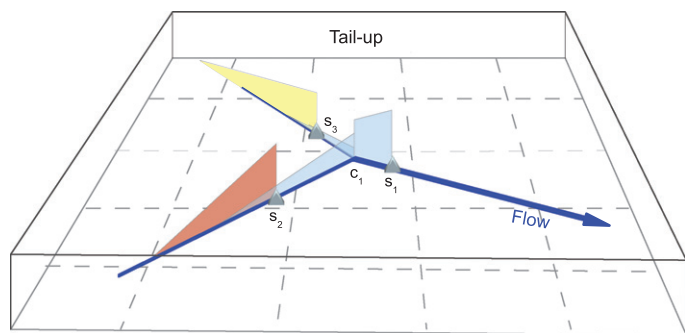
### Spatial statistical modelling on stream networks

Spatial statistical modelling is a well-established branch of statistics, which provides a convenient way to model spatially dependent data (Box 2). However, standard spatial statistical models may not adequately represent the unique spatial relationships found in stream networks and other DENs. For example, lattice models, which are used to model spatial dependency in aerial units, model autocovariance (i.e. autocorrelation) based on neighbourhoods, whereas Euclidean distance has typically been used to build autocovariance models in geostatistics (i.e. kriging; Cressie 1993). These metrics of distance and proximity do not reflect the influence of dendritic structure, connectivity and directionality within a network. In addition, a model is not guaranteed to be statistically valid when hydrologic distance is used in a geostatistical model developed for Euclidean distance in 2-D space (Ver Hoef *et al.* 2006).

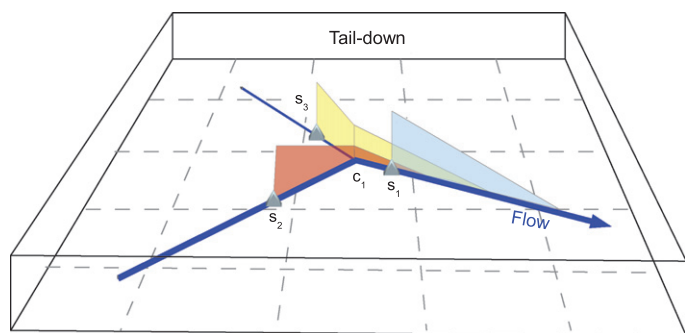
Ver Hoef & Peterson (2010) summarised the development of the tail-up and tail-down autocovariance models for stream networks (Cressie *et al.* 2006; Ver Hoef *et al.* 2006; Money *et al.* 2009a,b; Garreta *et al.* 2009), which are based on a branching, continuous spatial analogue to moving averages in time series. These models account for two types of spatial relationships based on hydrologic distance: flow-connected and flow-unconnected (Fig. 3). Two locations are considered flow-connected if water flows from the upstream location to the downstream location. Flow-unconnected locations reside on the same stream network (e.g. share a common confluence somewhere downstream), but do not share flow. Although the tail-up (Fig. 4) and tail-down (Fig. 5) models are both adapted for branching in streams and account for directionality, there are significant differences in the way that spatial relationships are represented in the two models. In the case of the 'tail-up' model, the tail of the moving-average function points in the upstream direction (Fig. 4). As a result, the function must be split at confluences to allow for



**Figure 3** There are two types of spatial relationships in a stream network: flow-connected and flow-unconnected. For two locations to be flow-connected, water must flow from an upstream location to a downstream location ( $S_3$  and  $S_1$ ,  $S_2$  and  $S_1$ ). Flow-unconnected locations share a common confluence (e.g. junction) somewhere downstream, but do not share flow ( $S_2$  and  $S_3$ ).



**Figure 4** The tail-up model points upstream from each location and restricts autocorrelation to flow-connected locations. The moving-average functions are shown in red, yellow and blue in the vertical dimension. Spatial autocorrelation occurs between locations when their moving-average functions overlap and the amount of overlap contributes to the magnitude of spatial correlation. The size of the stream (blue line) is proportional to the line width. A spatial-weighting scheme based on stream size is used to split the moving-average function at confluences ( $C_1$ ) so that locations on larger segments ( $S_2$ ) are more strongly correlated with downstream locations ( $S_1$ ) than locations on smaller segments ( $S_3$ ); even though the distance between  $S_3$  and  $S_1$  is shorter than the distance between  $S_2$  and  $S_1$ .



**Figure 5** The tail-down model allows spatial autocorrelation between both flow-connected and flow-unconnected locations. The moving-average functions are shown in red, yellow and blue in the vertical dimension. Spatial autocorrelation occurs between locations when the moving-average functions overlap and the amount of overlap contributes to the magnitude of spatial correlation. The moving-average function for the tail-down model points downstream from each location and so a spatial-weighting scheme is not needed to split the function at confluences ( $C_1$ ). The size of the stream (blue line) is proportional to its line width.

the disproportionate influence of one converging segment over another (e.g. a large stream segment converges with a smaller one) using flow volume or another ecologically influential variable. Information, such as flow volume, is rarely available for all segments in the network and so catchment area is often used as a surrogate for flow (e.g. Ruesch *et al.* 2012). Spatial autocorrelation occurs between locations when the moving-average functions overlap, and as a result, spatial autocorrelation only occurs between flow-connected locations in the tail-up model (Fig. 4). In contrast, the moving-average function for the tail-down model points in the downstream direction (Fig. 5). Notice there is overlap in the moving-average functions when two sites are flow-connected and flow-unconnected, so there is spatial autocorrelation in both situations. In addition, weights are not necessary because segments converge in the down-

stream direction. The tail-up correlation structure may be useful for modelling materials or organisms that move passively downstream, such as nutrients (Gardner & McGlynn 2009), while the tail-down models may be useful for modelling the abundance of organisms, such as fish, which have the capacity to actively move both up and downstream.

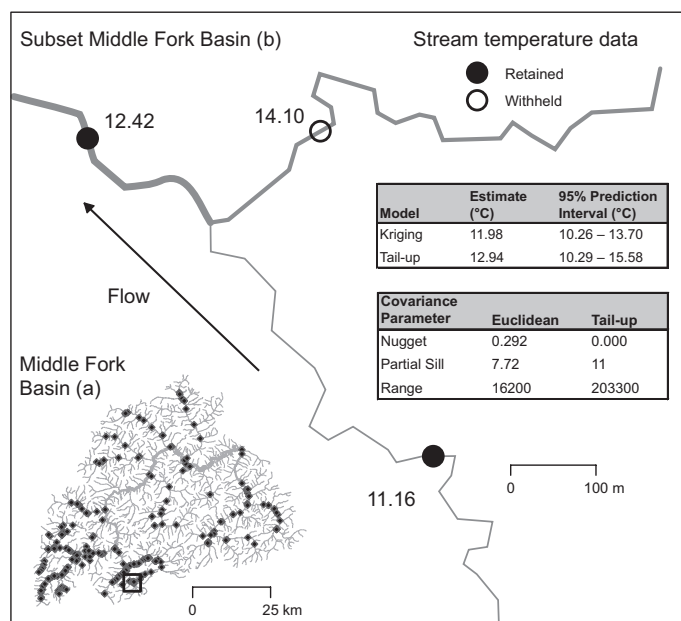
The need to quantify patterns of spatial autocorrelation that are best described in network space is intuitive in a DEN where the network structure is obvious. However, DENs are also embedded within 2-D space and complex, multi-scale processes and interactions occur across the dual coordinate system. This is especially true in stream ecosystems where topographic and climatic gradients (e.g. elevation and air temperature), as well as, land-management or disturbances within the catchment and riparian zone (e.g. tree cover or wildfires) have direct and indirect effects on physicochemical and biological in-stream processes (Isaak *et al.* 2010). Thus, it is not uncommon for stream data to show evidence of multiple Euclidean and/or hydrologic patterns of spatial autocorrelation (Peterson *et al.* 2006; Garreta *et al.* 2009). To address this issue, autocovariance models developed for Euclidean distance may be combined with stream-network models to produce mixed models based on variance components (Ver Hoef & Peterson 2010), through an extension of the spatial linear model:

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{z}_{TU} + \mathbf{z}_{TD} + \mathbf{z}_E + \boldsymbol{\varepsilon} \quad (2)$$

where  $\mathbf{y}$  is a vector of response variables,  $\mathbf{X}$  is a matrix of covariates,  $\boldsymbol{\beta}$  is a parameter vector,  $\mathbf{z}_{TU}$  and  $\mathbf{z}_{TD}$  are vectors of zero-mean random variables with a correlation structure based on the tail-up and tail-down stream-network models, respectively,  $\mathbf{z}_E$  is a vector of zero-mean random variables with a correlation structure based on Euclidean distance, and  $\boldsymbol{\varepsilon}$  is a vector of independent random errors (see Box 2 for an overview of the spatial linear-mixed model). When spatial random effects are added to form a mixed-covariance structure and then combined with covariates within a single model, a flexible modelling framework is formed that can be used to account for measured and unmeasured variables at multiple scales (Peterson & Ver Hoef 2010).

#### *Is it worth it?*

Creating a stream-network model involves more effort than employing standard geostatistical methods. Calculating hydrologic distances and spatial weights requires advanced GIS expertise, whereas the Euclidean distances can be calculated easily using site coordinates, with or without a GIS. So, how much is really gained by using spatially explicit on-network models? We explore this with a simple example from the Middle Fork of the Lower Snake River, Idaho (Fig. 6a). Daily stream temperatures were recorded in the summer of 2004 and summarised to produce a summer mean temperature for each location (Isaak, D.J., unpublished data). We fit two models to these data: (1) a standard geostatistical model using Euclidean distance with a constant mean (no covariates) and a spherical autocovariance model (i.e. ordinary kriging; Cressie 1993), and (2) a stream-network model, with a constant mean and a tail-up spherical autocovariance model (Ver Hoef *et al.* 2006). A small portion of the stream network (black square, Fig. 6a) is shown in Fig. 6b, which contains three locations labelled with the observed temperature values. First, we used all of the data locations shown in Fig. 6a to estimate the covariance parameters (nugget, partial sill, and range; Box 2) for both the standard geostatistical model and the tail-up



**Figure 6** (a) Daily stream temperatures (°C) were measured in the summer of 2004 throughout the Middle Fork Basin, USA and summarised to produce a mean summer temperature for each location ( $n = 90$ ). Two models were fit to these data: (1) a standard geostatistical model using Euclidean distance (i.e. kriging) and (2) a stream-network model (i.e. tail-up). (b) We withheld one datum and used the two neighbouring observed data points, as well as the fitted covariance parameters to make predictions at the withheld location.

stream-network model using restricted maximum likelihood; the covariance parameter estimates are shown in a Table in Fig. 6b. We then withheld one measurement and used the two observed data points, as well as the estimated covariance parameters to make predictions at the withheld location. Using ordinary kriging and the geostatistical methods based on Euclidean distance, the predicted value for the withheld location was 11.98 °C, with a 95% prediction interval of 10.26–13.70 °C. This interval does not capture the true value of 14.10 °C. In contrast, the tail-up stream-network model predicted a higher value of 12.94 °C, with a prediction interval of 10.29–15.58 °C, which captures the true value.

The network-based model yields a more accurate prediction because ordinary kriging generally interpolates between observed locations. From this perspective, the Euclidean model produces a sensible prediction of 11.98 °C, which lies between the two observed values and is more similar to the closer downstream location (Fig. 6b). Yet, this may not make sense for a flowing stream. Before we discuss the prediction made by the tail-up model, notice that the temperature increased from 11.16 °C to 12.42 °C downstream between the two observed locations (Fig. 6b). This suggests that the unobserved tributary added warm water, causing the rise in temperature. Logically, the downstream temperature of 12.42 °C should be some weighted average of temperatures from the two upstream segments; one has a temperature of 11.16 °C, and the other temperature is unknown, but is surely greater than 12.42 °C. Thus, the kriging estimate of 11.98 °C is not sensible, whereas the estimate from the stream-network model, 12.94 °C, is much more reasonable. Furthermore, the prediction intervals provided by the tail-up model are wider, which better reflects the uncertainty coming

from the physical structure of the network, rather than the interpolation based on Euclidean distance.

This simple example clearly demonstrates the potential benefits of implementing a spatial stream-network model. However, these benefits only materialise when (1) the data are spatially correlated, (2) spatial autocorrelation is best described using a hydrologic (e.g. flow-connected or flow-unconnected) rather than Euclidean relationship and (3) data are distributed across a branching network rather than a single, non-branching stream channel. In addition, the spatial distribution of survey sites has important implications on the number of neighbouring pairs used to fit the autocovariance function (Peterson *et al.* 2006; Box 2). If there are too few flow-connected or flow-unconnected locations, there is little to gain from fitting a spatial stream-network model.

### Generalised linear models and other extensions

Non-Gaussian data, such as counts of organisms or species presence-absence, are commonly collected for monitoring programs and ecological studies. Spatial linear models may be applied to non-Gaussian data if transformations are used to normalise the response and homogenise the variance. However, another approach is the generalised linear model (GLM), which uses Poisson or binomial distributions directly, and this approach has already been adapted for spatial statistical models based on Euclidean distance (Diggle *et al.* 1998). To our knowledge, spatial GLMs using stream-network models as reviewed by Ver Hoef & Peterson (2010) have not been described in the literature, but in principle stream-network covariances can be used in GLMs in exactly the same way as Euclidean distance covariances are used; consequently, no new methodological developments are needed to fit a spatial GLM for stream networks.

### Empirical semivariogram analysis and the Torgegram

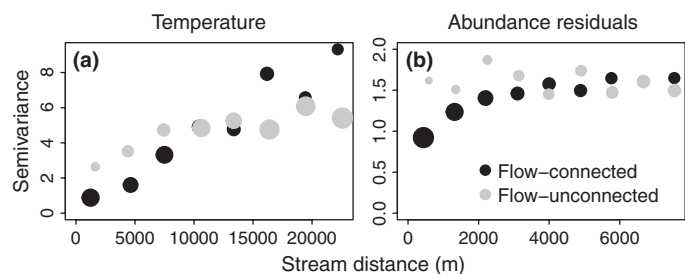
Empirical semivariogram analysis is used to explore how the spatial dependence between observations changes as a function of distance. These patterns may be particularly interesting in stream networks, where the dendritic structure, as well as longitudinal and lateral connectivity can produce multiple patterns of spatial autocorrelation (Peterson & Ver Hoef 2010). An empirical semivariogram estimates the semivariance ( $0.5 \times \text{var}(Y_i - Y_j)$  for all  $i \neq j$ ) plotted as a function of increasing distance among observed locations, where pairwise distances (i.e. separation distances) are aggregated into bins. Empirical semivariograms that display a patterned increase in semivariance with increasing distance indicate that the data, or model residuals, exhibit positive spatial autocorrelation.

In the case of stream-network processes, a Torgegram (Ver Hoef *et al.* in review) is used to display semivariance as a function of hydrologic distance separately for flow-connected and flow-unconnected relationships (Fig. 3); making them useful exploratory tools for visualising different network-based patterns of spatial autocorrelation in raw data or model residuals, which we illustrate next using two examples.

#### *The Torgegram: Visualising network-based patterns of spatial autocorrelation*

We constructed a Torgegram using 178 mean summer stream temperature observations (Fig. 7a) collected in the Bear Valley Creek catchment (13,000 km<sup>2</sup>), upper Middle Fork of the Salmon River, Idaho, USA (Isaak, D.J., unpublished data), assuming a constant





**Figure 7** The Torgegram is used to display semivariance as a function of hydrologic distance separately for flow-connected and flow-unconnected relationships, with the size of the circle proportional to the number or paired locations used to estimate the semivariance. The two Torgegrams shown here are based on (a) raw stream temperature data collected in the upper Middle Fork Salmon River, USA and (b) juvenile rainbow trout abundance data collected in the Elk River catchment, USA.

mean among all locations. The second Torgegram (Fig. 7b) relies on 386 juvenile *Oncorhynchus mykiss* (rainbow trout) abundance data collected in the Elk River catchment (238 km<sup>2</sup>), located in southwestern Oregon, USA (Burnett 2001). The Torgegram in Fig. 7b was constructed using residuals from a spatial linear model where abundance values were first log<sub>e</sub> transformed, and a regression coefficient for trend in upstream distance was estimated using model covariates. Three parameters are used to describe the shape of the semivariogram: the nugget effect, the sill, and the range (Box 2). For stream temperature, there can be only one overall sill, which appears to be around 5. The nugget effect for flow-connected sites is near zero and the semivariance increases more slowly towards the sill (Fig. 7a), which suggests that the range of spatial correlation for flow-connected stream temperature sites may be near 15,000 m, or greater. In contrast, the flow-unconnected pairs exhibit a larger nugget effect and the semivariance increases more rapidly to a range of approximately 10,000 m. These characteristics suggest that the data exhibit both flow-connected and flow-unconnected patterns of spatial autocorrelation and that fitting a mixed-covariance structure that includes both tail-up and tail-down autocorrelation models may be appropriate. A relatively strong pattern of spatial autocorrelation between flow-connected pairs is also evident in the Torgegram for the abundance residuals (Fig. 7b); the nugget effect is approximately 0.8 for flow-connected sites, with a sill near 1.6, and a range approaching 4,000 m. Yet, the semivariance for the flow-unconnected pairs does not appear to change as a function of hydrologic distance, which suggests that flow-unconnected locations may not be spatially correlated after accounting for the upstream trend. As such, adding a single tail-up autocorrelation model might be sufficient.

### Abundance estimation and block kriging

Estimates of averages or totals, along with their estimated precision, **over** stream networks, sub-networks or stream segments are particularly important for managing populations of aquatic organisms or monitoring pollution impacts. For example, Poos *et al.* (2012) derived sub-catchment-scale population estimates of *Clinostomus elongates* (reidside dace), an endangered minnow, by extrapolating pool-scale density estimates based on a combination of quantitative and qualitative rules. These pool and sub-catchment-scale estimates were then used to better understand the relationship between the distri-

bution of reidside dace and impervious land use. Classical approaches to abundance estimation use exhaustive surveys to minimise bias and achieve reasonable precision, which increases the cost of sampling and limits the survey area (e.g. Hankin & Reeves 1988). Classical random-sampling techniques can also be used, such as simple or stratified-random sampling, but lack predictive ability and precision for small areas. In addition, it may not be feasible to truly randomise sample placement due to a lack of access (e.g. no roads, steep canyons or uncooperative land owners). Even if a randomised design can be used, there may be better estimators, such as block prediction, or universal block kriging on stream networks (Ver Hoef *et al.* 2006), to scale up from an **on-** to an **over-**network analysis.

### Future research

The full suite of spatial statistical models described thus far, including mixed models, spatial GLMs and block kriging on stream networks, may be fit using the SSN package (Ver Hoef *et al.* in review) for R statistical software (R Development Core Team 2010). However, other methods would also be useful and more research is needed to make them spatially explicit on stream networks. For example, incomplete-detection occupancy models (MacKenzie *et al.* 2002) provide a way to estimate occupancy rates from binary data, while also accounting for the probability of detection. Analysis of extremes for water quality often involves converting continuous data to a binary response at the threshold level (Clement & Thas 2009) or using generalised extreme-value models that depend on a distribution (Towler *et al.* 2010). Analyses at broad scales may lead to computational issues with large sample sizes (e.g. in-stream sensor networks, Porter *et al.* 2012); therefore, spatial statistical methods for large data sets, such as fixed-rank kriging (Cressie & Johannesson 2008), could be adapted for stream networks. Current methods only account for spatial dependency in stream data, but there is clearly a temporal-dynamic structure that should be incorporated simultaneously using spatio-temporal analytic methods (Cressie & Wikle 2011). Finally, inferences for spatial data are substantially affected by the spatial configuration of survey sites on the network (Zimmerman 2006). Many survey designs seek spatial balance over the geographical range (Stevens & Jensen 2007), but proximity and connectivity in stream networks are functionally different than in terrestrial systems, requiring research on stream-specific survey designs to optimise objectives.

### INTEGRATING NETWORK ANALYSES

Previous network analyses in stream ecosystems have focused on the influence of either network-explicit variables (e.g. physical network structure and flow direction) or network-implicit variables (e.g. continuous, hierarchical and spatio-temporally heterogeneous in-stream habitat quality). However, the tendency to focus solely on either spatial structure or function is not unique to stream ecology and there has been an effort to integrate disparate perspectives to gain a more holistic understanding of the study system (Paola *et al.* 2006; Rodríguez-Iturbe *et al.* 2009). For example, Massol *et al.* (2011) noted that much of the research on spatial food webs in ecology has been developed independently from research on ecosystem dynamics, and proposed a 'metaecosystem' framework for bringing concepts from landscape ecosystem and food-web meta-community ecology together. In another study, Jabot & Bascompte

(2012) demonstrated how a metacommunity model, which focuses on spatial processes in a single trophic group, could be integrated with a network model that considers multiple trophic groups at a single location, to obtain a better understanding of how network structure affects metacommunity dynamics. The combined influence of spatial structure and ecological interactions on in- or near-stream processes is also of interest in stream ecology (Angermeier *et al.* 2002; Power & Dietrich 2002; Fisher *et al.* 2004; Falke & Fausch 2010), but the dual coordinate system makes explicitly accounting for their combined influence more complicated than in other spatially structured ecological networks.

The taxonomy of network analyses provides a framework to aid in the integration of different models preferred by ecological subdisciplines, such as community, landscape or population ecology. As a first step, studies that include both **on-** and **about-**network analyses, potentially within a single statistical framework, are relatively straightforward to implement and will provide a means of investigating the influence of in-stream habitat availability *and* physical network structure on the distribution of organisms. For example, a spatial statistical model could be used to generate semi-continuous predictions of in-stream habitat based on physical sub-network structure or other remotely derived covariates, such as climate, topography or land cover. Then, **about-**network metrics could be used to relate the configuration and connectivity of predicted habitat patches to species distributions using a graph-theoretic-based model. Different types of **on-**network analyses may also be combined to address more complex questions. Goldberg *et al.* (2010) developed a matrix population model to investigate the effects of dendritic network structure and within-network habitat patches on species distributions. Habitat patch characteristics were assigned based on distance upstream from the stream outlet; however, a spatial statistical model could be used to estimate more realistic segment-scale habitat characteristics (e.g. temperature or substrate type) thought to influence organismal dispersal, survival or reproduction, based on catchment land-management practices. These examples demonstrate how spatial statistical methods can be used to predict biologically relevant information at an intermediate scale (1–100 km), which can then be combined with **about-** or **on-**network analyses; thus, accounting for the interplay between network structure, within-network habitat characteristics or processes, and/or the characteristics of the 2-D landscape the network resides within.

The ability to integrate various network analyses in DENs also opens the door to a suite of previously intractable research questions. For example, cutthroat trout is a species of concern in the northwestern United States, where their distribution is relatively limited compared to historical distributions (Young 1995). Evidence suggests that these declines may be due to habitat degradation (Harig *et al.* 2000), isolation of populations (Haak *et al.* 2010) and competition with invasive species such as *Salvelinus fontinalis* (brook trout; Fausch 2008). It remains unclear, however, which factors are responsible for most of the decline, and whether their influence is spatially heterogeneous or varies depending on scale. An integrated approach using both **on-** and **about-**network methods provides a way to investigate each component's respective contribution, as well as, its influence on other ecological dynamics. This information could then be used to develop a network-explicit reserve design (Urban *et al.* 2009) or to undertake a risk or cost–benefit analysis to identify areas with the greatest conservation or restoration potential (Urban & Keitt 2001). Other taxa of concern also share

habitat with cutthroat trout (e.g. *Dicamptodon sp.*) and a spatially structured network model (Jabot & Bascompte 2012) would provide a way to move from single species conservation to a multispecies approach (Urban *et al.* 2009). In addition, air and stream water temperatures are expected to increase in the future, causing shifts in fish distributions (Hari *et al.* 2006), which adds to the challenge of spatially explicit, conservation prioritisation efforts. One solution would be to study potential metacommunity dynamics using time-ordered networks (Blonder *et al.* 2012) under a series of future climate and thermal habitat scenarios to account for new species interactions, as well as, changes in habitat quality and network structure resulting from lower stream flows. Finally, ecological processes (e.g. movement and dispersal) are often facilitated or impeded by non-natural transport mechanisms such as human reintroductions and the intercatchment transfer of water, nutrients or organisms (Fullerton *et al.* 2011; Grant *et al.* 2012). Thus, there is a need to understand the effects of these human-imposed networks on physically constrained networks, such as DENs. The taxonomy of network analyses provides a conceptual framework to select and combine complimentary analytical methods to understand complex ecological systems composed of both physicochemical and biological processes that operate across multiple scales in the dual coordinate system.

#### OTHER DENs AND SPATIALLY STRUCTURED ECOLOGICAL NETWORKS

Although our primary focus has been on stream ecology (Box 1), the conceptual taxonomy of network analyses is relevant for any dendritic ecological network, which exists within a dual coordinate system. The same concepts and models could be used to select and combine analyses of preferential, but not exclusive, use and migration of terrestrial or semi-aquatic species along riparian corridors (Naiman & Décamps 1997; Carranza *et al.* 2012); the effects of both pollution and the distribution of refugia on fauna in cave networks (Wood *et al.* 2008); or studies investigating the effects of plant architecture on foraging intensity or pest infestation patterns in dendritically structured plants (Legrand & Barbosa 2003; Sylvaine *et al.* 2012). For example, spatial statistical methods have previously been used to explore pest and nutrient distributions in trees (Habib *et al.* 1991; Audergon *et al.* 1993) and the tail-down covariance model would be particularly suited for these problems. In addition, a model based on a covariance mixture (i.e. tail-down, tail-up and Euclidean) would allow complex patterns of spatial autocorrelation associated with proximity to the plant's main stem or differences in light exposure to be accounted for, in addition to those associated with network structure.

The taxonomy of network analyses would also be relevant in other ecological settings where processes are not limited to Euclidean space, but rather follow pathways that are constrained by the physical environment. For example, the effects of ocean currents on larval dispersal (Hidalgo *et al.* 2011); patterns of dissolved oxygen in estuaries (Rathbun 1998); animal movement along habitat corridors (Castellón & Sieving 2006); and plant (Spooner *et al.* 2004) and animal dispersal along road networks (Brock & Kelt 2004). Note that, the specific models and examples provided here may not be suitable in every situation (e.g. a spatial statistical model for stream networks cannot be applied to a non-dendritic road network). Nevertheless, other models found within the same families of models, such as

spatial statistical methods, graph-theoretic approaches and metapopulation models, can be combined in a myriad of ways to systematically account for the interplay between network structure, within-network characteristics or processes, and the characteristics of the 2-D landscape the network resides within.

## SUMMARY

Dendritic ecological networks, such as streams ecosystems, are a unique form of spatially structured ecological network that play a vital role in ecology (Paola *et al.* 2006). Analytical methods that explicitly account for fundamental characteristics, such as network structure and connectivity within the dual coordinate system, are needed to better understand the processes governing physicochemical and biological properties within DENs and the surrounding environment. This is especially true in streams, where longitudinal connectivity strongly influences in-stream processes and lateral connectivity blurs the boundary between the aquatic and terrestrial environment (Fisher *et al.* 2004). If the fundamental characteristics of DENs are not accounted for in the analyses, it can lead to poor scientific inference, and in turn, poor management decisions. Therefore, the ability to account for these fundamental characteristics within an analytical framework is especially important for bridging the gap between research pertaining to fine-scale processes and broad-scale management decisions (Fausch *et al.* 2002).

We proposed a unifying taxonomy of analyses **non-**, **about-**, **on-**, **over-** and **across-** networks to help researchers (1) understand the differences between the processes of interest and the analytical methods available, (2) select the most suitable method for their study and (3) integrate network analyses to acquire a more coherent system-wide understanding. We then considered **on-**network analysis in more detail because it has received the least attention and there have been recent novel developments, while the taxonomy of network analyses provided the context for such development. There are undoubtedly other analytical methods that were not discussed, which account for network characteristics to varying degrees, such as process-based models used to predict sediment movement in streams (Gassman *et al.* 2007) or network-explicit spatial optimisation methods used to prioritise conservation efforts (Hermoso *et al.* 2011). Nevertheless, the taxonomic framework allows ecologists to place other methods, including those yet to be developed, within the broader context of potential network analyses.

Our hope is that this taxonomic framework will help ecologists quantitatively embrace the spatial complexity of DENs, as well as, explore and test the evolving ecological conceptualisation of DENs as a unique form of spatially structured ecological network. Interdisciplinary collaboration between ecologists and statisticians made it possible to develop this framework. Further cross-disciplinary collaboration is needed to ensure that new statistical methods represent the fundamental characteristics of spatially structured ecological networks, so that ecologists can push the boundaries of their science, while also providing managers with tools for solving real-world problems.

## ACKNOWLEDGEMENTS

This study was conducted as part of the Spatial Statistics for Streams Working Group supported by the National Center for Ecological Analysis and Synthesis, a Center funded by the National

Science Foundation (Grant #EF-0553768), the University of California, Santa Barbara and the State of California. We thank G.H. Reeves and K.M. Burnett at the US Forest Service Pacific Northwest Research Station for providing the rainbow trout abundance data used to develop the Torgegram in Fig. 7b. We also thank Frederieke Kroon, Nick Bond, Dan Pagendam and three anonymous reviewers for constructive comments on previous versions of this manuscript. Note that, any use of trade, product, or firm names is for descriptive purposes only and does not imply endorsement by the US Government.

## AUTHORSHIP

This manuscript was developed as part of the National Center for Ecological Analysis and Synthesis, Spatial Statistics for Streams working group and all authors provided major contributions to its conceptual development. The first three authors contributed portions of text, synthesised contributions from co-authors, developed examples and provided general editing. The remaining authors wrote portions of text, developed examples, contributed to editing and/or provided feedback on previous versions of the manuscript; these authors are listed in alphabetical order.

## REFERENCES

- Angermeier, P.L. & Krueger, K.L. & Dolloff, C.A. (2002). Discontinuity in stream-fish distributions: Implications for assessing and predicting species occurrence. In: *Predicting Species Occurrences: Issues of Accuracy and Scale* (eds Scott, J.M., Heglund, P., and Morrison, M.L.). Island Press, Covelo, CA, U.S.A., pp. 519–527.
- Audergon, J.-M., Monestiez, P. & Habib, R. (1993). Spatial dependences and sampling in a fruit tree: A new concept for spatial prediction in fruit studies. *J. Hortic. Sci.*, 68, 99–112.
- Auerbach, D.A. & Poff, N.L. (2011). Spatio-temporal controls of simulated metacommunity dynamics in dendritic networks. *J. N. Am. Benthol. Soc.*, 30, 235–251.
- Barr, T.C. Jr & Holsinger, J.R. (1985). Speciation in cave faunas. *Ann. Rev. Ecol. Syst.*, 16, 313–337.
- Bascompte, J., Melián, C.J. & Sala, E. (2005). Interaction strength combinations and the overfishing of a marine food web. *Proc. Natl. Acad. Sci. USA*, 102, 5443–5447.
- Benda, L., Poff, N.L., Miller, D., Reeves, G., Pess, G. & Pollock, M. (2004). The Network Dynamics Hypothesis: How channel networks structure riverine habitats. *Bioscience*, 54, 413–427.
- Blonder, B., Wey, T.W., Dornhaus, A. & James, R. & Sih, A. (2012). Temporal dynamics and network analysis. *Method. Ecol. Evol.*, 3, 958–972.
- Brock, R.E. & Kelt, D.A. (2004). Influence of roads on the endangered Stephens' kangaroo rat (*Dipodomys stephensi*): are dirt and gravel roads different? *Biol. Conserv.*, 118, 633–640.
- Burnett, K.M. (2001). Relationships among juvenile anadromous salmonids, their freshwater habitat, and landscape characteristics over multiple years and spatial scales in Elk River, Oregon. Ph.D. Dissertation. Oregon State University, Corvallis, Oregon, USA.
- Cadotte, M.W. (2006). Competition-colonization trade-offs and disturbance effects at multiple scales. *Ecology*, 88, 823–829.
- Carranza, M.L., D'Alessandro, E., Saura, S. & Loy, A. (2012). Connectivity providers for semi-aquatic vertebrates: The case of the endangered otter in Italy. *Landscape Ecol.*, 27, 281–290.
- Carrara, F., Altermatt, F., Rodríguez-Iturbe, I. & Rinaldo, A. (2012). Dendritic connectivity controls biodiversity patterns in experimental metacommunities. *Proc. Natl. Acad. Sci. USA*, 109, 5761–5766.
- Castellón, T.D. & Sieving, K.E. (2006). An experimental test of matrix permeability and corridor use by an endemic understory bird. *Conserv. Biol.*, 20, 135–145.

- Clement, L. & Thas, O. (2009). Testing for trends in the violatin frequency of an environmental threshold in rivers. *Environmetrics*, 20, 53–67.
- Cote, D., Kehler, D.G., Bourne, C. & Wiersma, Y.F. (2009). A new measure of longitudinal connectivity for stream networks. *Landscape Ecol.*, 24, 101–113.
- Cressie, N. (1993). *Statistics for Spatial Data*. Revised edn. John Wiley & Sons, New York.
- Cressie, N. & Johannesson, G. (2008). Fixed rank kriging for very large spatial data sets. *J. R. Stat. Soc. B*, 70, 209–226.
- Cressie, N. & Wikle, C.K. (2011). *Statistics for Spatio-temporal Data*. John Wiley & Sons, Hoboken.
- Cressie, N., Frey, J., Harch, B. & Smith, M. (2006). Spatial prediction on a river network. *J. Agric. Biol. Environ. Stat.*, 11, 127–150.
- Cressie, N., Calder, K.A., Clark, J.S., Ver Hoef, J.M. & Wikle, C.K. (2009). Accounting for uncertainty in ecological analysis: The strengths and limitations of hierarchical statistical modeling. *Ecol. Appl.*, 19, 553–570.
- Dale, M.R.T. & Fortin, M.-J. (2010). From graphs to spatial graphs. *Annu. Rev. Ecol. Evol. Syst.*, 41, 21–38.
- Diggle, P.J., Tawn, J.A. & Moyeed, R.A. (1998). Model-based geostatistics. *J. R. Stat. Soc. C-App.*, 47, 299–350.
- Dunham, J.B. & Rieman, B.E. (1999). Metapopulation structure of bull trout: influences of physical, biotic, and geometrical landscape characteristics. *Ecol. Appl.*, 8(9), 642–655.
- Erös, T., Schmera, D. & Schick, R.S. (2011). Network thinking in riverscape conservation – a graph-based approach. *Biol. Conserv.*, 144, 184–192.
- Fagan, W.F. (2002). Connectivity, fragmentation, and extinction risk in dendritic metapopulations. *Ecology*, 83, 3243–3249.
- Falke, J.A. & Fausch, K.D. (2010). From metapopulations to metacommunities: linking theory with empirical observations of the spatial population dynamics of stream fishes. (eds Gido, K.B. and Jackson, D.A.). American Fisheries Society Special Publication, 73, 207–233.
- Fall, A., Fortin, M.-J., Manseau, M. & O'Brien, D. (2007). Spatial graphs: Principles and applications for habitat connectivity. *Ecosystems*, 10, 448–461.
- Fausch, K.D. (2008). A paradox of trout invasions in North America. *Biol. Invasions*, 10, 685–701.
- Fausch, K.D., Torgersen, C.E., Baxter, C.V. & Li, H.W. (2002). Landscapes to riverscapes: bridging the gap between research and conservation of stream reaches. *Bioscience*, 52, 483–498.
- Finlay, J., Hood, J.M., Limm, M.P., Power, M.E., Schade, J.D. & Welter, J.R. (2011). Light-mediated thresholds in stream-water nutrient composition in a river network. *Ecology*, 92, 140–150.
- Fisher, S.G. (1997). Creativity, idea generation, and the functional morphology of streams. *J. N. Am. Benthol. Soc.*, 16, 305–318.
- Fisher, S.G., Sponseller, R.A. & Heffernan, J.B. (2004). Horizons in stream biogeochemistry: Flowpaths to progress. *Ecology*, 85, 2369–2379.
- Flitcroft, R.L., Burnett, K.M., Reeves, G.H. & Ganio, L.M. (2012). Do network relationships matter? Comparing network and instream habitat variables to explain densities of juvenile coho salmon (*Oncorhynchus kisutch*) in mid-coastal Oregon, USA. *Aquat. Conserv.*, 22, 288–302.
- Fortuna, M.A., Albaladejo, R.G., Fernandez, L., Aparicio, A. & Bascompte, J. (2009). Networks of spatial genetic variation across species. *Proc. Natl. Acad. Sci. USA*, 106, 19044–19049.
- Fullerton, A.H., Lindley, S.T., Pess, G.R., Feist, B.E., Steel, E.A. & McElhany, P. (2011). Human influence on the spatial structure of threatened Pacific salmon metapopulations. *Conserv. Biol.*, 25, 932–944.
- Ganio, L.M., Torgersen, C.E. & Gresswell, R.E. (2005). A geostatistical approach for describing spatial pattern in stream networks. *Front. Ecol. Environ.*, 3, 138–144.
- Gardner, K.K. & McGlynn, B.L. (2009). Seasonality in spatial variability and influence of land use/land cover and watershed characteristics on stream water nitrate concentrations in a developing watershed in the Rocky Mountain West. *Water Resour. Res.*, 45, W08411.
- Garreta, V., Monestiez, P. & Ver Hoef, J.M. (2009). Spatial modeling and prediction on river networks: up model, down model, or hybrid. *Environmetrics*, 21, 439–456.
- Gassman, P.W., Reyes, M.R., Green, C.H. & Arnold, J.G. (2007). The Soil and Water Assessment Tool: Historical development, applications, and future research directions. *Trans. ASABE*, 50, 1211–1250.
- Gilarranz, L.J. & Bascompte, J. (2012). Spatial network structure and metapopulation persistence. *J. Theor. Biol.*, 297, 11–16.
- Goldberg, E.E., Lynch, H.J., Neubert, M.G. & Fagan, W.F. (2010). Effects of branching spatial structure and life history on the asymptotic growth rate of a population. *Theor. Ecol.*, 3, 137–152.
- Grant, E.H.C., Lowe, W.H. & Fagan, W.F. (2007). Living in the branches: population dynamics and ecological processes in dendritic networks. *Ecol. Lett.*, 10, 165–175.
- Grant, E.H.C., Lynch, H.J., Muneeppeerakul, R., Arunachalam, M. & Rodríguez-Iturbe, I. & Fagan, W.F. (2012). Interbasin water transfer, riverine connectivity, and spatial controls on fish biodiversity. *PLoS ONE*, 7, e34170.
- Haak, A.L., Williams, J.E., Neville, H.M., Dauwalter, D.C. & Colyer, W.T. (2010). Conserving peripheral trout populations: The values and risks of life on the edge. *Fisheries*, 35, 530–549.
- Habib, R., Tisne-Agostini, D., Vanniere, M.-P. & Monestiez, P. (1991). Geostatistical method for independent in kiwifruit vine to estimate yield components. *New Zeal. J. Crop Hort.*, 19, 329–335.
- Hankin, D.G. & Reeves, G.H. (1988). Estimating total fish abundance and total habitat area in small streams based on visual estimation methods. *Can. J. Fish. Manage.*, 45, 834–844.
- Hanski, I. (1998). Metapopulation dynamics. *Nature*, 396, 41–49.
- Hari, R.E., Livingstone, D.M., Siber, R., Burkhardt-Holm, P. & Güttinger, H. (2006). Consequences of climatic change for water temperature and brown trout populations in Alpine rivers and streams. *Glob. Change Biol.*, 12, 10–26.
- Harig, A.L., Fausch, K.D., and Young, M.K. (2000). Factors influencing Success of Greenback Cutthroat Trout Translocations. *N. Am. J. Fish. Manage.*, 20, 994–1004.
- Hermoso, V., Linke, S., Prenda, J. & Possingham, H.P. (2011). Addressing longitudinal connectivity in the conservation planning of fresh waters. *Freshwater Biol.*, 56, 57–70.
- Hidalgo, T., Gusdal, M.Y., Dingsor, G.E., Hjermmann, D., Ottersen, G., Stige, L.C. et al. (2011). A combination of hydrodynamical and statistical modelling reveals non-stationary climate effects on fish larvae distributions. *Proc. R. Soc. Biol. Sci.*, 279, 275–283.
- Hitt, N.P. & Angermeier, P.L. (2008). River-stream connectivity affects fish bioassessment performance. *Environ. Manage.*, 42, 132–150.
- Horton, R.E. (1945). Erosional development of streams and their drainage basins; hydrophysical approach to quantitative morphology. *Geol. Soc. Am. Bull.*, 56, 275–370.
- Isaak, D.J., Thurow, R.F., Rieman, B.E. & Dunham, J.B. (2007). Relative roles of habitat quality, size, and connectivity in Chinook salmon use of spawning patches. *Ecol. Appl.*, 17, 352–364.
- Isaak, D.J., Luce, C.H., Rieman, B.E., Nagel, D.E., Peterson, E.E., Horan, D.L. et al. (2010). Effects of climate change and wildfire on stream temperatures and salmonid thermal habitat in a mountain river network. *Ecol. Appl.*, 20, 1350–1371.
- Jabot, F. & Bascompte, J. (2012). Biotrophic interactions shape biodiversity in space. *Proc. Natl. Acad. Sci. USA*, 109, 4521–4526.
- Kolaczyk, E.D. (2009). *Statistical Analysis of Network Data*. Springer Series in Statistics, New York.
- Le Pichon, C., Gorges, G., Boët, P., Baudry, J., Goreaud, F. & Thierry, F. (2006). A spatially explicit resource-based approach for managing stream fishes in riverscapes. *Environ. Manage.*, 37, 322–335.
- Legendre, P. & Fortin, M.-J. (2010). Comparison of the Mantel test and alternative approaches for detecting complex multivariate relationships in the spatial analysis of genetic data. *Mol. Ecol. Resour.*, 10, 831–844.
- Legrand, A. & Barbosa, P. (2003). Plant morphological complexity impacts foraging efficiency of adult *Coccinella septempunctata* L. (Coleoptera: Coccinellidae). *Environ. Entomol.*, 32, 1219–1226.
- MacKenzie, D.I., Nichols, J.D., Lachman, G.B., Droege, S., Royle, J.A. & Langtimm, C.A. (2002). Estimating site occupancy rates when detection probabilities are less than one. *Ecology*, 83, 2248–2255.
- Mantel, N. (1967). The detection of disease clustering and a generalized regression approach. *Cancer Res.*, 27, 209–220.

- Massol, F., Gravel, D., Mouquet, N., Cadotte, M.W., Fukami, T. & Leibold, M.A. (2011). Linking community and ecosystem dynamics through spatial ecology. *Ecol. Lett.*, 14, 313–323.
- Money, E., Carter, G. & Serre, M.L. (2009a). Modern space/time geostatistics using river distances: data integration of turbidity and *E. coli* measurements to assess fecal contamination along the Raritan River in New Jersey. *Environ. Sci. Technol.*, 43, 3736–3742.
- Money, E., Carter, G. & Serre, M.L. (2009b). Using river distance in the space/time estimation of dissolved oxygen along two impaired river networks in New Jersey. *Water Res.*, 43, 1948–1958.
- Muneepeerakul, R., Bertuzzo, E., Rinaldo, A. & Rodríguez-Iturbe, I. (2008). Patterns of vegetation biodiversity: The roles of dispersal directionality and river network structure. *J. Theor. Biol.*, 252, 221–229.
- Naiman, R.J. & Décamps, H. (1997). The ecology of interfaces: riparian zones. *Annu. Rev. Ecol. Syst.*, 28, 621–658.
- Pandey, P.K., Soupir, M.L., Haddad, M. & Rothwell, J.J. (2012). Assessing the impacts of watershed indexes and precipitation on spatial in-stream *E. coli* concentrations. *Ecol. Indic.*, 23, 641–652.
- Paola, C., Foufoula-Georgiou, E., Dietrich, W.E., Hondzo, M., Mohrig, D., Parker, G. *et al.* (2006). Toward a unified science of the Earth's surface: Opportunities for synthesis among hydrology, geomorphology, geochemistry, and ecology. *Water Resour. Res.*, 42, W03S10.
- Peterson, E.E. & Ver Hoef, J.M. (2010). A mixed-model moving-average approach to geostatistical modeling in stream networks. *Ecology*, 91, 644–651.
- Peterson, E.E., Merton, A.A., Theobald, D.M. & Urquhart, N.S. (2006). Patterns of spatial autocorrelation in stream water chemistry. *Environ. Monit. Assess.*, 121, 569–594.
- Poos, M., Lawrie, D., Tu, C., Jackson, D.A. & Mandrak, N.E. (2012). Estimating local and regional population sizes for an endangered minnow, redbreast dace (*Clinostomus elongates*), in Canada. *Aquat. Conserv.*, 22, 47–57.
- Porter, H.J., Hanson, P.C. & Lin, C.C. (2012). Staying afloat in the sensor data deluge. *Trends Ecol. Evol.*, 27, 121–129.
- Power, M.E. & Dietrich, W.E. (2002). Food webs in river networks. *Ecol. Res.*, 17, 451–471.
- Proulx, S.R., Promislow, D.E.L. & Phillips, P.C. (2005). Network thinking in ecology and evolution. *Trends Ecol. Evol.*, 20, 345–353.
- R Development Core Team (2010). *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria. Available at: <http://www.R-project.org/>.
- Rathbun, S.L. (1998). Spatial modeling in irregularly shaped regions: Kriging estuaries. *Environmetrics*, 9, 109–129.
- Rayfield, B., Fortin, M.-J. & Fall, A. (2011). Connectivity for conservation: A framework to classify network measures. *Ecology*, 92, 847–858.
- Rodríguez-Iturbe, I., Muneepeerakul, R., Bertuzzo, E., Levin, S.A. & Rinaldo, A. (2009). River networks as ecological corridors: A complex systems perspective for integrating hydrologic, geomorphologic, and ecological dynamics. *Water Resour. Res.*, 45, W01413.
- Ruesch, A.S., Torgersen, C.E., Lawler, J.J., Olden, J.D., Peterson, E.E., Volk, C.J. *et al.* (2012). Projected climate-induced habitat loss for salmonids based on a network model of stream temperature. *Conserv. Biol.*, 26, 873–882.
- Sanderson, B.L., Barnas, K.A. & Wargo-Rub, A.M. (2009). Nonindigenous species of the Pacific Northwest: An overlooked risk to endangered salmon? *Bioscience*, 59, 245–256.
- Schick, R.S. & Lindley, S.T. (2007). Directed connectivity among fish populations in a riverine network. *J. Appl. Ecol.*, 44, 1116–1126.
- Schlosser, I.J. & Angermeier, P.L. (1995). Spatial variation in demographic processes in lotic fishes: Conceptual models, empirical evidence, and implications for conservation. *American Fisheries Society Symposium*, 17, 360–370.
- Smouse, P.E., Long, J.C. & Sokal, R.R. (1986). Multiple regression and correlation extensions of the Mantel test of matrix correspondence. *Syst. Zool.*, 35, 627–632.
- Spoooner, P.G., Lunt, I.D., Okabe, A. & Shiode, S. (2004). Spatial analysis of roadside *Acacia* populations on a road network using the network K-function. *Landscape Ecol.*, 19, 491–499.
- Stevens, D.L. Jr & Jensen, S.F. (2007). Sample design, execution, and analysis for wetland assessment. *Wetlands*, 27, 515–523.
- Sylvaine, S., Morel, K., Durand, E., Brevalle, G., Girard, T. & Lauri, P. (2012). Aphids at crossroads: when branch architecture alters aphid infestation patterns in the apple tree. *Trees*, 26, 273–282.
- Towler, E., Rajagopalan, B., Gilleland, E., Summers, R.S., Yates, D. & Katz, R.W. (2010). Modeling hydrologic and water quality extremes in a changing climate: a statistical approach based on extreme value theory. *Water Resour. Res.*, 46, W11504.
- Urban, D. & Keitt, T. (2001). Landscape connectivity: A graph-theoretic perspective. *Ecology*, 82, 1205–1218.
- Urban, D.L., Minor, E.S., Treml, E.A. & Schick, R.S. (2009). Graph models of habitat mosaics. *Ecol. Lett.*, 12, 260–273.
- Ver Hoef, J.M. & Peterson, E.E. (2010). A moving average approach for spatial statistical models of stream networks. *J. Am. Stat. Assoc.*, 105, 6–18. Rejoinder: 22–24.
- Ver Hoef, J.M., Peterson, E.E. & Theobald, D. (2006). Spatial statistical models that use flow and stream distance. *Environ. Ecol. Stat.*, 13, 449–464.
- Ver Hoef, J.M., Peterson, E.E. & Clifford, D. & Shah, R. (in review). SSN: an R package for spatial statistical modeling on stream networks. Submitted to *J. Stat. Softw.* Available at: <http://www.fs.fed.us/rm/boise/AWAE/projects/SpatialStreamNetworks.shtml>
- Vörösmarty, C.J., McIntyre, P.B., Gessner, M.O., Dudgeon, D., Prusevich, A., Green, P. *et al.* (2010). Global threats to human water security and river biodiversity. *Nature*, 467, 555–561.
- Ward, J.V. (1998). Riverine landscapes: biodiversity patterns, disturbance regimes, and aquatic conservation. *Biol. Conserv.*, 83, 269–278.
- Wiens, J.A. (2002). Riverine landscape: taking landscape ecology into the water. *Freshwater Biol.*, 47, 501–515.
- Wood, P.J., Gunn, J. & Rundle, S.D. (2008). Response of benthic cave invertebrates to organic pollution events. *Aquat. Conserv.*, 18, 909–922.
- Young, M.K. (1995). *Conservation Assessment for Inland Cutthroat Trout. General Technical Report RM-256*. U.S. Department of Agriculture, Forest Service, Rocky Mountain Forest and Range Experiment Station Fort Collins, CO, U.S.A.
- Yuan, L.L. (2004). Using spatial interpolation to estimate stressor levels in unsampled streams. *Environ. Monit. Assess.*, 94, 23–38.
- Zimmerman, D. (2006). Optimal network design for spatial prediction, covariance parameter estimation, and empirical prediction. *Environmetrics*, 17, 635–652.

Editor, Bernd Blasius

Manuscript received 19 September 2012

First decision made 31 October 2012

Manuscript accepted 14 January 2013